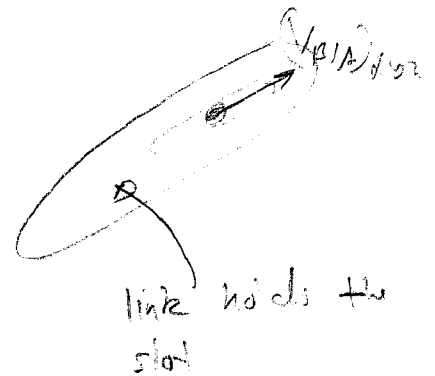


20.4 Relative Motion Analysis Using Rotating & Translating axes

Points on the same body have relative motion ^{section}

⇒ The same as chapter 16.5.

Attach (x, y, z) to the body that contains the relative motion.
 $\vec{\omega}$ is the angular velocity of (x, y, z) which is the same as $\vec{\omega}$ of the body.



Velocity

$$\Rightarrow \vec{V}_B = \vec{V}_A + \vec{\omega} \times \vec{r}_{B/A} + (\vec{V}_{B/A})_{xyz}$$

acceleration

$$\begin{aligned} \vec{a}_B = \vec{a}_A + \vec{\omega} \times \vec{r}_{B/A} + \vec{\omega} \times (\vec{\omega} \times \vec{r}_{B/A}) \\ + 2\vec{\omega} \times (\vec{V}_{B/A})_{xyz} + (\vec{a}_{B/A})_{xyz} \end{aligned}$$

Problem 20-47

$\vec{V}_T$? $\vec{a}_T$

$$\begin{aligned} \vec{V}_C = \vec{V}_D = \vec{V}_A = -8\hat{i} \text{ m/s} \\ \vec{a}_C = \vec{a}_D = \vec{a}_A = -9\hat{i} \text{ m/s}^2 \end{aligned}$$

$$\vec{V}_T = \vec{V}_A + \vec{\omega}_{AB} \times \vec{r}_{T/A} + (\vec{V}_T)_{xyz}$$

$$\vec{\omega}_{AB} = \vec{\omega}_1 + \vec{\omega}_2 = 0.5\hat{k} + 0.4\hat{i}$$

$$\begin{aligned} \Rightarrow \vec{V}_T = -8\hat{i} + (0.4\hat{i} + 0.5\hat{k}) \times 8\hat{j} + 3\hat{j} \\ = -8\hat{i} + 1.2\hat{k} - 1.5\hat{i} + 3\hat{j} = (-9.5\hat{i} + 3\hat{j} + 1.2\hat{k}) \text{ m/s} \end{aligned}$$

$$\vec{a}_T = \vec{a}_A + \vec{\omega}_{AB} \times \vec{r}_{T/A} + \vec{\omega}_{AB} \times (\vec{\omega}_{AB} \times \vec{r}_{T/A}) + (\vec{a}_T)_{xyz} + 2\vec{\omega}_{AB} \times (\vec{V}_T)_{xyz}$$

$$\vec{\omega}_{AB} = \vec{\omega}_1 + \vec{\omega}_2 = (\vec{\omega}_1)_{xyz} + (\vec{\omega}_2)_{xyz} + \vec{\omega}_1 \times \vec{\omega}_2 = 0.8\hat{k} + 0.6\hat{i} + \frac{(0.5\hat{k} \times 0.4\hat{i})}{0.2\hat{j}}$$

$$\begin{aligned} \Rightarrow \vec{a}_T = -9\hat{i} + (0.6\hat{i} + 0.2\hat{j} + 0.8\hat{k}) \times (8\hat{j}) + (0.4\hat{i} + 0.5\hat{k}) \times (1.5\hat{i} + 1.2\hat{k}) + 3\hat{j} + 2(0.4\hat{i} + 0.5\hat{k}) \times 3\hat{j} \\ = -9\hat{i} + 1.8\hat{k} - 2.4\hat{i} - 0.48\hat{j} - 0.75\hat{j} + 5\hat{j} + 2.4\hat{k} - 3\hat{i} \\ = (-9 - 2.4 - 3)\hat{i} + (-0.48 - 0.75 + 5)\hat{j} + (1.8 + 2.4)\hat{k} \\ = -14.4\hat{i} + 3.77\hat{j} + 4.2\hat{k} \end{aligned}$$

