



Lecture 19

Bonds

Types of Financing

◆ Cash (owners' capital):

- Private funds
- Partnerships
- Stocks

◆ Debt (loans, bonds):

- ***Bonds are just one type of financing!***

◆ Leasing

When to Borrow

- ◆ **Better than other options in long run:**
 - E.g., higher present value
- ◆ **Suitable payment plan in short run:**
 - Less flexible than selling stock
- ◆ **Loans difficult in volatile industries:**
 - But can increase rate of return to owners
 - ◆ *Can increase return without larger investment!*

Types of Loans

- ◆ **Interest each year, principal at end:**
 - **Bonds**
- ◆ **Annual payments of principal:**
 - **Equal principal, declining interest**
 - **Equal total, increasing principal (car/house)**
- ◆ **No interest each year, interest/principal at end (some federal bonds)**

Types of loans

- ◆ **All are equivalent *if*:**
 - **Life of debt = Life of asset**
 - **Interest rate of debt = minimum acceptable rate of return**
- ◆ **Minimum acceptable rate of return typically $>$ interest rate:**
 - **Loan period may also be $<$ asset life**
 - **E.g., cars**

Definitions

◆ Face value:

- Lump-sum amount that will be paid at end
- *Not necessarily equal to purchase price!*

◆ Interest payment:

- $(\text{Face value}) \times (\text{Interest rate}) / (\# \text{ periods})$

◆ *Coupon rate* = interest rate

Bond Repayment

- ◆ **If collecting capital to repay bonds:**
 - **Must be in a safe investment**
(sinking fund)
 - **(Interest rate may be less than the rate on the loan!)**
- ◆ **Can buy back bonds early:**
 - **Depends on price**

Bond Repayment

❖ Alternative approach:

- ***Serial maturity***
 - ◆ (e.g., issue bonds due in years 1-20)
- **Can buy back at face value (guaranteed!)**
 - ◆ But no flexibility on timing
- **Often used by local governments:**
 - ◆ Tax income is fairly stable
 - ◆ ***Prevents diversion of accumulated funds!***

Example

◆ Typical bond:

- 7% interest rate
- \$10,000 face value
- Due in 20 years
- Compounded every 6 months
 - ◆ Need to use effective interest rate!

◆ Buying this bond is like loaning the company \$10,000 for 20 years!

Example (continued)

◆ Bond owner gets:

- Interest of \$350 every 6 months
- \$10,000 in 20 years

◆ How much is this bond worth?

- Minimum acceptable rate of return is 9%, compounded semi-annually

Example (continued)

◆ Present worth of bond:

- $\$350$ (P/A, 4.5%, 40) = $\$6,441$
- $\$10,000$ (P/F, 4.5%, 40) = $\$1,719$
- Total = $\$8,160$

◆ Would not pay more than $\$8,160$

◆ Company borrows $\$8,160$:

- *Pays back $\$10,000!$*

Example (continued)

- ◆ **At a minimum attractive rate of return of 7%:**
 - **Bond would be worth exactly \$10,000**
- ◆ **At a minimum attractive rate of return of 4%:**
 - **Bond would be worth \$14,103**
 - ◆ *Loan company \$14,000*
 - ◆ *Get back only \$10,000*
 - **This is a good idea if no other investment pays more than 4%!**

Observations

- ◆ **Price is essentially a present value:**
 - So present value is better than equivalent annual cost for determining prices
- ◆ **If the current interest rate is **higher** than the coupon rate on the bond:**
 - The sale price will be **less** than face value
- ◆ **If the current interest rate is **lower**:**
 - The sale price will be **more** than face value!

Internal Rate of Return

- ◆ Find internal rate of return of bond:
 - 7% interest rate
 - \$10,000 face value
 - Due in 20 years
 - Compounded every 6 months
 - *Bought for \$8,000*
 - ◆ Can't do without knowing purchase price!
- ◆ Expect higher or lower than 7%?

Internal Rate of Return

- ◆ **At a minimum acceptable rate of return of 4.5% every 6 months:**
 - Present worth = \$8,160
- ◆ **At a minimum acceptable rate of return of 5% every 6 months:**
 - Present worth = \$7,426
- ◆ **To get present worth = \$8,000:**
 - Interpolation gives 4.6% per 6 months
 - Nominal interest rate of 9.2% per year

Internal Rate of Return

◆ For the investor:

- A large internal rate of return is *good!*
- (Large return on initial investment)

◆ For the company selling the bonds:

- A large internal rate of return is *bad!*
- Large future payments due
- Small initial influx of funds

Buyer versus Seller

- ◆ **Company sells \$50 million of bonds**
 - 9.2% interest rate
 - Due in 20 years
 - Compounded every 6 months
- ◆ **A total of 5,000 bonds are sold:**
 - Each with \$10,000 face value
 - ***Bought for \$9,750!***

Buyer versus Seller (continued)

- ◆ **Value to investors = 9.5% (yield):**
 - \$48.75 million initial investment
 - \$4.6 million in annual interest payments
 - ◆ (9.2% times \$50 million)
 - \$50 million in year 20
- ◆ **Cost to company \geq 9.8%:**
 - Larger than value to investors
 - Large rate of return is *bad* for seller!

Buyer versus Seller (continued)

- ◆ Minimum cost to company = 9.8%:
 - Present benefit $P = \$47.45$ million
 - *Sold to middlemen (investment bankers)!*
- ◆ Annual cost $A = \$4.6$ million
- ◆ Future cost $F = \$50$ million in year 20

Buyer versus Seller (continued)

◆ **More realistic cost to company 10.2%:**

- **Present benefit P = \$47.45 million**
 - ◆ **Minus \$0.85 million in setup costs**
 - ◆ **= \$46.6 million**
- **Annual cost A = \$4.6 million**
 - ◆ **Plus \$0.09 million in processing costs**
 - ◆ **= \$4.69 million**
- **Future cost F = \$50 million in year 20**

Observation

- ◆ **Income tax may make a difference:**
 - ***Interest payments are tax deductible!***
- ◆ **This analysis has been before tax**

Review

- ◆ We learned how to analyze bonds:
 - How to find maximum purchase price
 - ◆ Given a minimum acceptable rate of return
 - How to find internal rate of return (**yield**)
 - ◆ Given purchase price
- ◆ We learned how to interpret internal rate of return:
 - For investor, large rate of return is **good**
 - For seller, large rate of return is **bad**
 - ◆ (Cost of money!)